



# Filtration analysis of pedestrian-vehicle interactions for autonomous vehicle control

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# Team

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Techno-anthropology

# Motivations



EU City mobil 2 project

Trials of an AV:  
La Rochelle (France) and Trikala (Greece)

Finding from Madigan et al.:  
pedestrians intentionally step in front of the AV once every 3 hours



EU H2020 interACT project

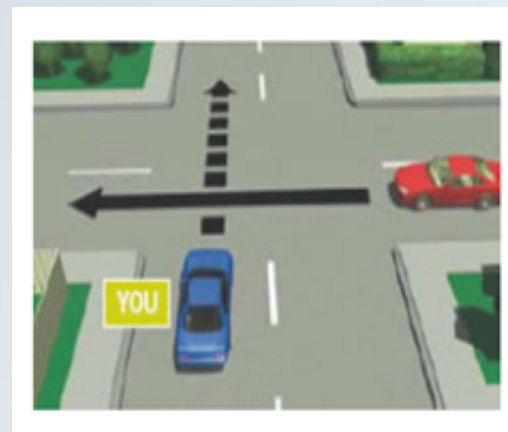


# Background

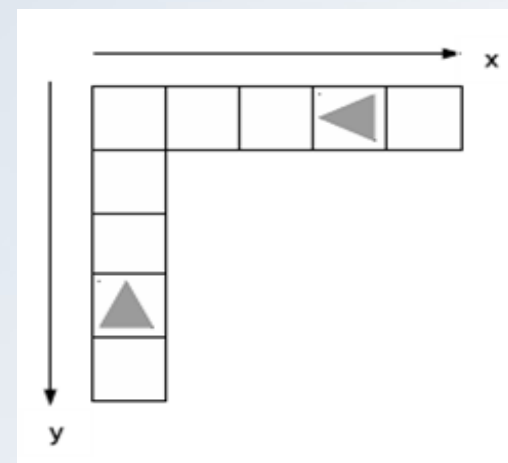
- Sequential Chicken Game: Game theory model for pedestrian-vehicle interactions
- Non-zero probability for a collision to occur
- Fit parameters  $U_{\text{crash}}$  and  $U_{\text{time}}$  to H-H interactions



Real world pedestrian-pedestrian interactions  
Between Hollywood and Highland, Los Angeles



Fox et al. 2018



Camara et al. 2018

# Data collection: Pedestrian-Vehicle interactions



Observers' standing locations (X and Y)

Intersection near Woodhouse Lane, University of Leeds

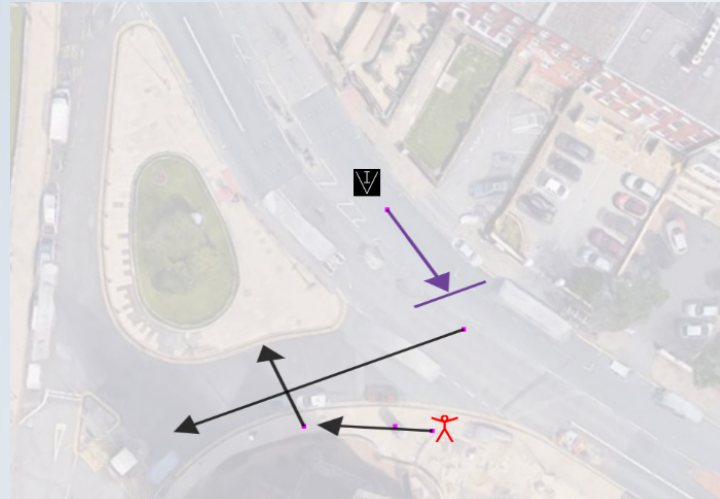
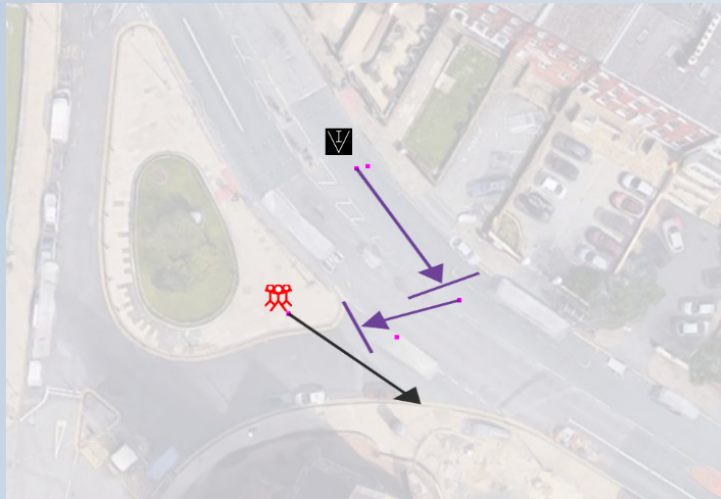
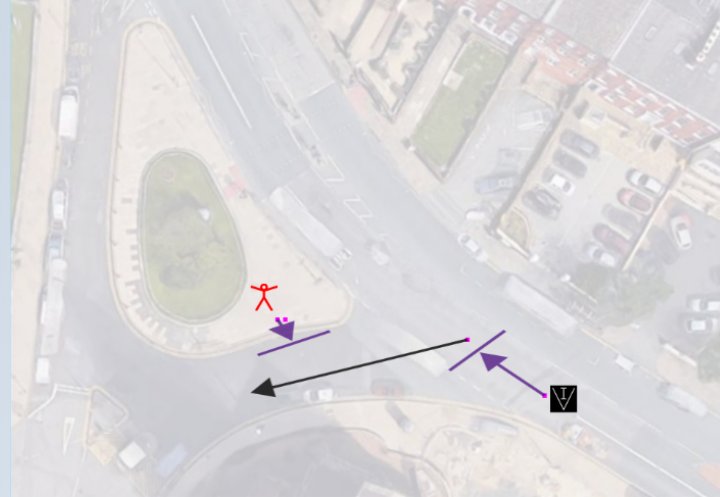
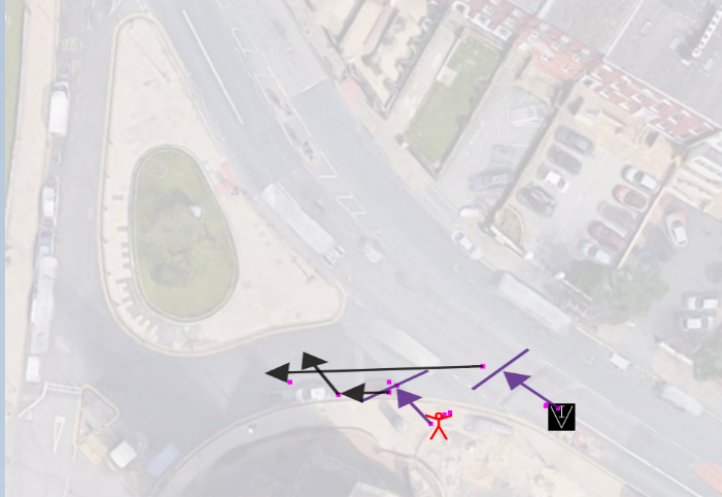
- 2 Observers standing next each other:
- one focusing on the pedestrian
  - the other focusing on the vehicle

Descriptor Features:  
gender, age, weather, number of  
pedestrian and vehicle, pedestrian's  
distraction


Event Features:  
(what is the pedestrian/vehicle doing ?)

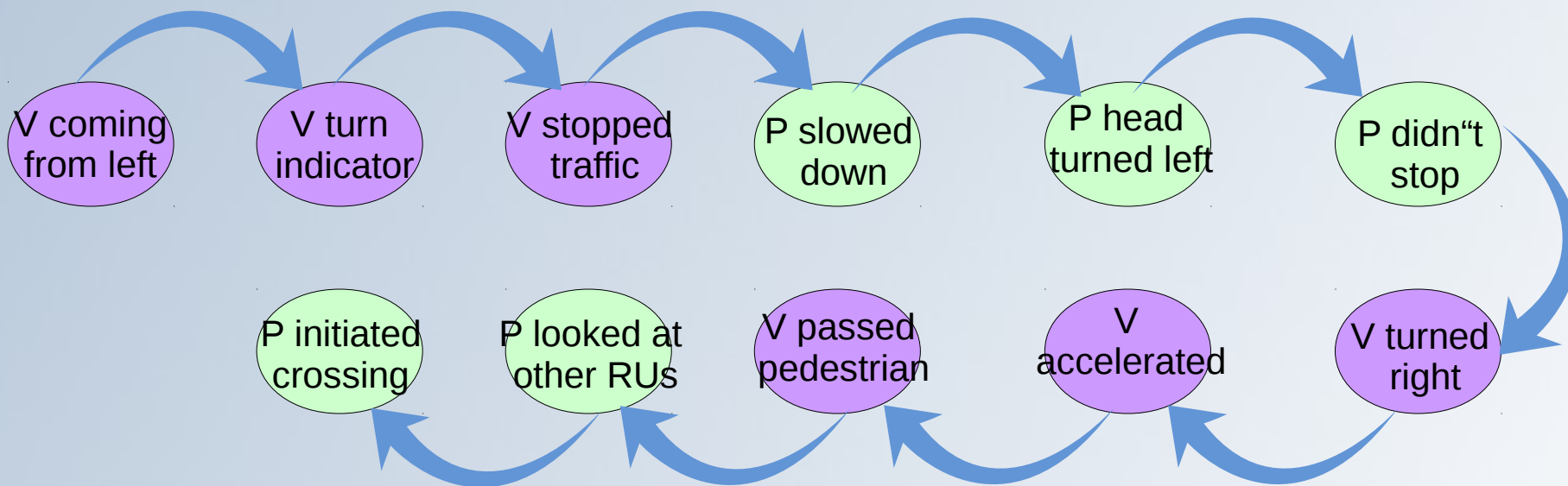
Approaching while keeping pace, stopped to due  
the traffic, turning the head to the right, using the  
turn indicator, looking at other road users, etc

# Examples of interactions



# Interactions

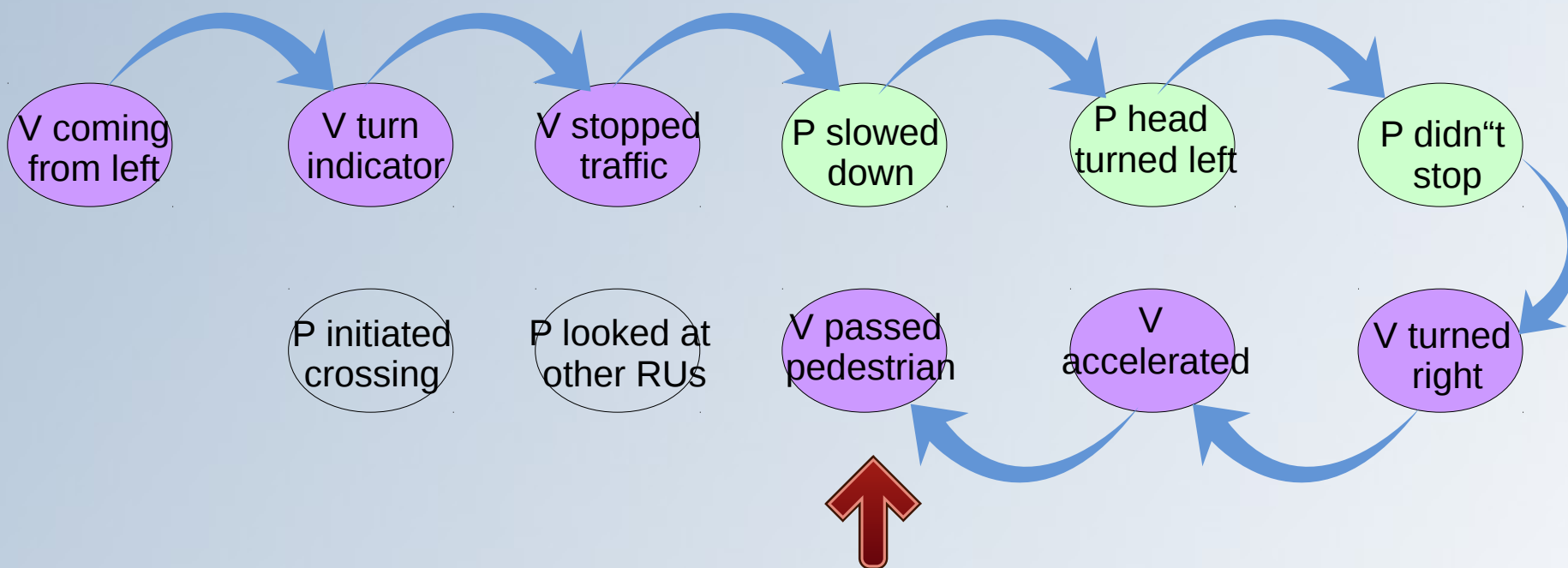
- 204 interactions  204 sequences of actions
- Example: a sequence of an interaction



P: Pedestrian  
V: Vehicle

# Interactions into games

- Game: Vehicle or Pedestrian winner ?

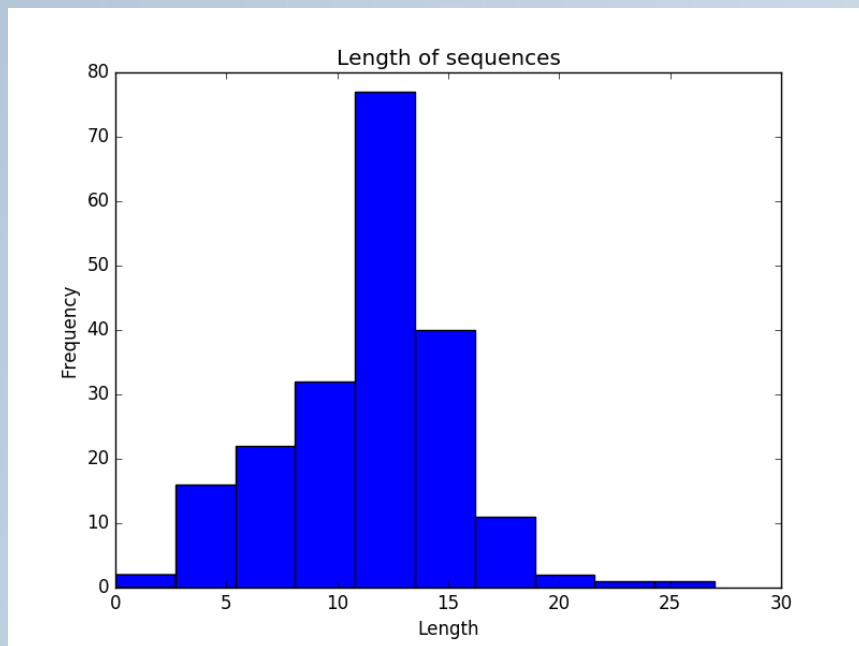


End of game event: vehicle winner of the interaction

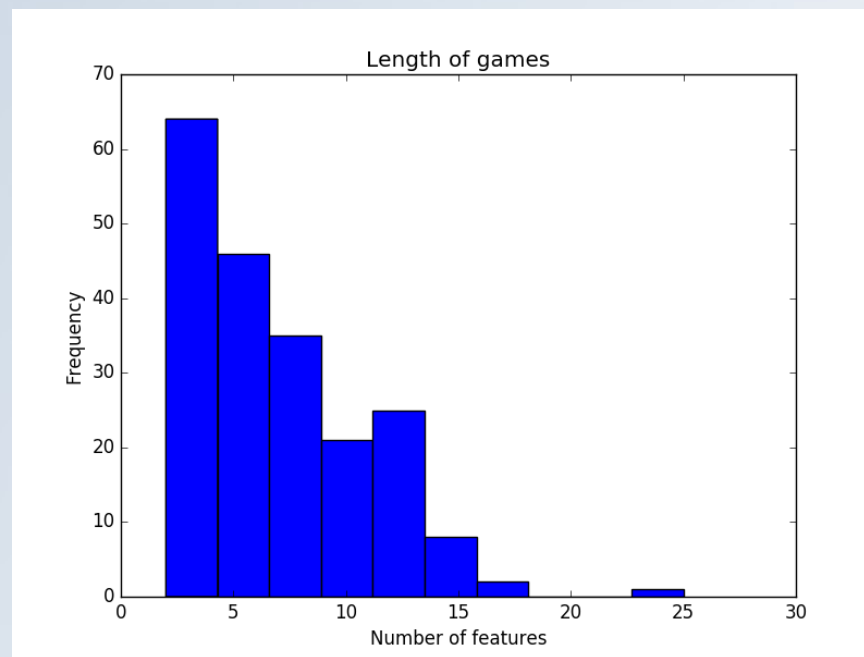
P: Pedestrian  
V: Vehicle



# Interactions vs Games



Interactions



Games

# Filtration

- Concept to incorporate events over time, used in optimal stopping problems  
e.g: Marriage problem, Biology (sequence analysis), Finance

- Compute likelihood for each descriptor/event features

$$\lambda(W|f_i) = \frac{\text{freq}(W|f_i)}{\text{freq}(W|f_i) + \text{freq}(\neg W|f_i)}$$



- Fuse likelihoods over time

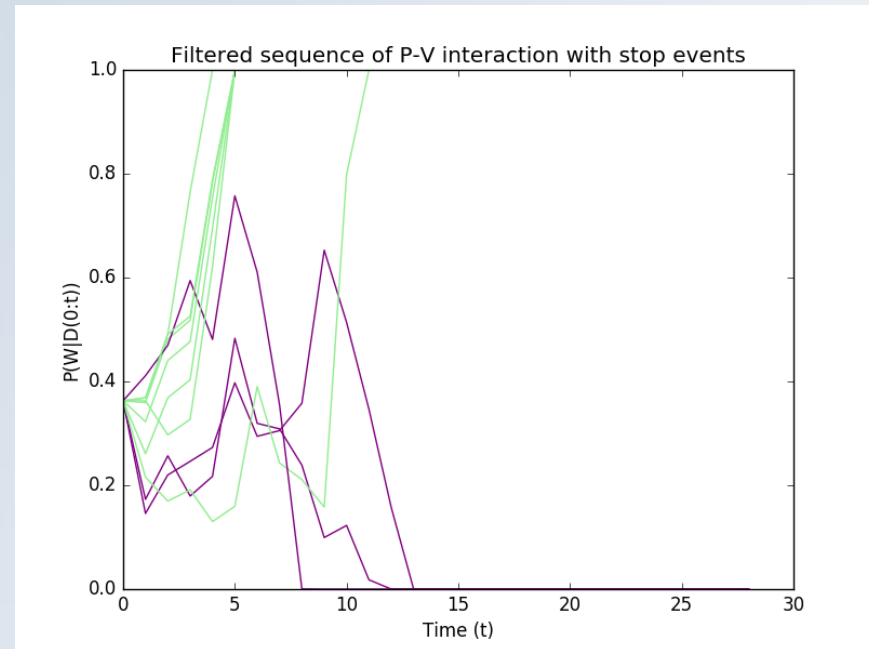
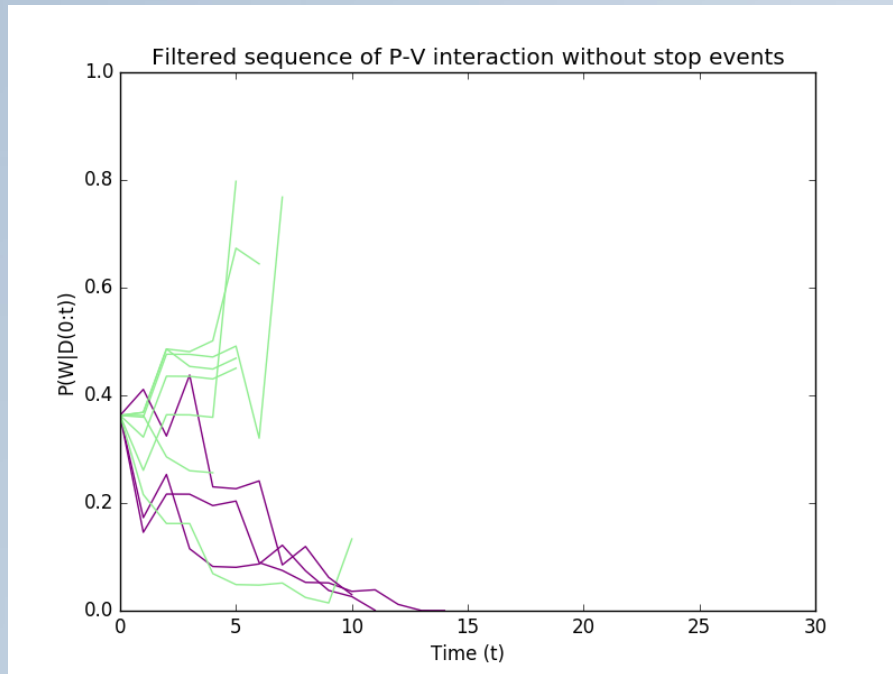
$$P(W|f_1, f_2, f_n) = P(W|0) \otimes \lambda(W|f_1) \otimes \lambda(W|f_2) \otimes \dots \otimes \lambda(W|F_n)$$

where  $p \otimes q = \frac{pq}{pq + (1-p)(1-q)}$

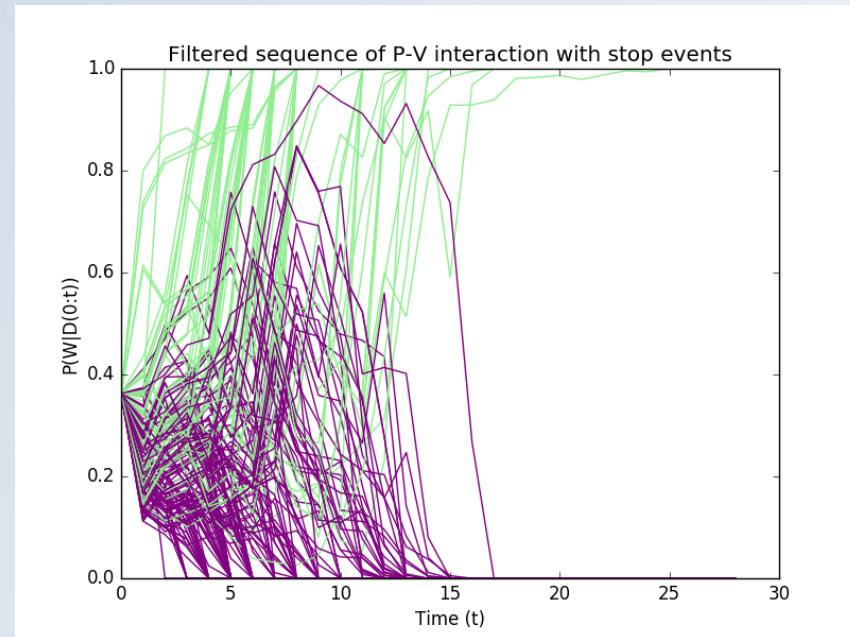
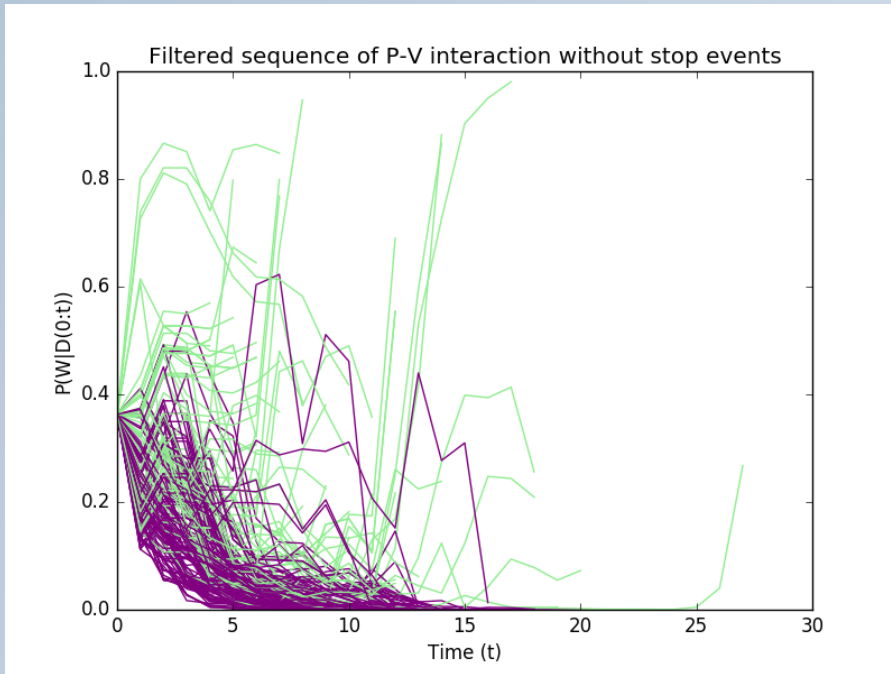
- ➔ t=0 : prior P(W|0) (36%: 74 out of 204)
- ➔ t=1 : all descriptors are observed and incorporated
- ...
- ➔ t=n : all features have been observed

Event Features $e_i$	$\lambda(W e_i)$
'Crossing Phase: Pedestrian Speeded up'	0.95471
'Crossing Phase: Driver/Vehicle Decelerated for observed pedestrian'	0.84051
'Crossing Phase: Driver/Vehicle Used signals Turn Indicator'	0.77844
'Approaching Phase: Driver/Vehicle Waved hand'	0.77844
'Approaching Phase: Driver/Vehicle Head Movements Other (elaborate in notes)'	0.7784
'Crossing Phase: Driver/Vehicle Movement Other (elaborate in notes)'	0.77844
'Crossing Phase: Pedestrian Raised hand in front'	0.77844
'Crossing Phase: Driver/Vehicle Raised hand in front'	0.7784
'Crossing Phase: Driver/Vehicle Head Turned in the direction of pedestrian'	0.7784
'Crossing Phase: Driver/Vehicle Stopped for observed pedestrian'	0.7784
'Crossing Phase: Pedestrian Looked at driver'	0.7784
'Approaching Phase: Driver/Vehicle Stopped due to other pedestrian'	0.7784
'Crossing Phase: Pedestrian Movements Other (elaborate in notes)'	0.77844
'Crossing Phase: Pedestrian Initiated crossing movement'	0.7712
'Approaching Phase: Driver/Vehicle Head Turned in the direction of pedestrian'	0.74541
'Crossing Phase: Pedestrian Head Movements Turned left'	0.7454
'Approaching Phase: Driver/Vehicle Interacting vehicle Bus / Truck'	0.72490
'Approaching Phase: Vehicle Stopped for observed pedestrian'	0.7008
'Crossing Phase: Pedestrian Looking at other pedestrians entering the road'	0.6372
'Crossing Phase: Pedestrian Waved Hand'	0.63725
'Approaching Phase: Driver/Vehicle Head Turned left'	0.6372
'Approaching Phase: Driver/Vehicle Movement Other (elaborate in notes)'	0.6372
'Approaching Phase: Pedestrian Hand Movements Other (elaborate in notes)'	0.6372
'Crossing Phase: Driver/Vehicle Turned left'	0.6372
'Crossing Phase: Vehicle Waved hand'	0.63725
'Crossing Phase: Driver/Vehicle Accelerated'	0.63725
'Crossing Phase: Driver/Vehicle Turned right'	0.6372
'Approaching Phase: Pedestrian Looking at other pedestrians entering the road'	0.6372
'Approaching Phase: Pedestrian Looking at other RUs Others (elaborate in notes)'	0.6372
'Approaching Phase: Driver/Vehicle Used signals Flashed Lights'	0.6372
'Approaching Phase: Pedestrian Movements Kept pace'	0.6231
'Approaching Phase: Vehicle Used signals Turn Indicator'	0.559
'Crossing Phase: Driver/Vehicle Passed the pedestrian'	0.5394
'Approaching Phase: Pedestrian Movements Did not Stop'	0.5365
'Approaching Phase: Pedestrian Head Movements Turned right'	0.53485
'Approaching Phase: Driver/Vehicle approached From left'	0.5292
'Approaching Phase: Driver/Vehicle Decelerated due to other pedestrians'	0.5131
'Approaching Phase: Driver/Vehicle Stopped due to traffic'	0.51315
'Approaching Phase: Driver/Vehicle approached from Multiple'	0.5009
'Approaching Phase: Driver/Vehicle Decelerated for observed pedestrian'	0.4875
'Approaching Phase: Pedestrian Speeded up'	0.46762
'Crossing Phase: Pedestrian Raised hand sideways'	0.4676
'Approaching Phase: Driver/Vehicle Interacting vehicle Other (elaborate in Notes)'	0.4676
'Crossing Phase: Pedestrian Stepped back on pavement'	0.4676
'Approaching Phase: Driver/Vehicle Turned left'	0.45419
'Approaching Phase: Pedestrian Stopped at the edge of the pavement'	0.43844
'Approaching Phase: Pedestrian Stepped on road and stopped'	0.42951
'Approaching Phase: Pedestrian Head Movements Turned left'	0.42951
'Approaching Phase: Pedestrian Movements Slowed down'	0.4260
'Crossing Phase: Pedestrian Looking at Looked at vehicle'	0.41269
'Approaching Phase: Driver/Vehicle Decelerated due to traffic'	0.3874
'Crossing Phase: Pedestrian Hand Movements Other (elaborate in notes)'	0.36931
'Approaching Phase: Driver Head Turned right'	0.36931
'Approaching Phase: Driver/Vehicle Interacting vehicle Van'	0.3693
'Approaching Phase: Driver/Vehicle Kept pace'	0.36931
'Approaching Phase: Driver/Vehicle Turned right'	0.3598
'Crossing Phase: Pedestrian Head Movements Turned right'	0.3341
'Approaching Phase: Pedestrian Looked at approaching vehicle'	0.3129
'Crossing Phase: Pedestrian Looking at other RUs (elaborate in comments)'	0.26
'Crossing Phase: Pedestrian Slowed down / stopped'	0.26
'Approaching Phase: Driver/Vehicle Accelerated'	0.163316
'Approaching Phase: Driver/Vehicle Passed the pedestrian'	0.11514

# Filtration results for 10 interactions



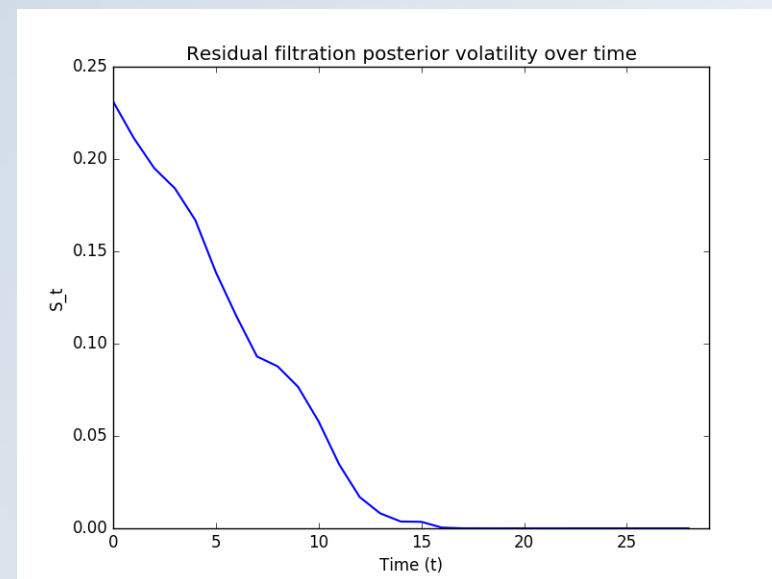
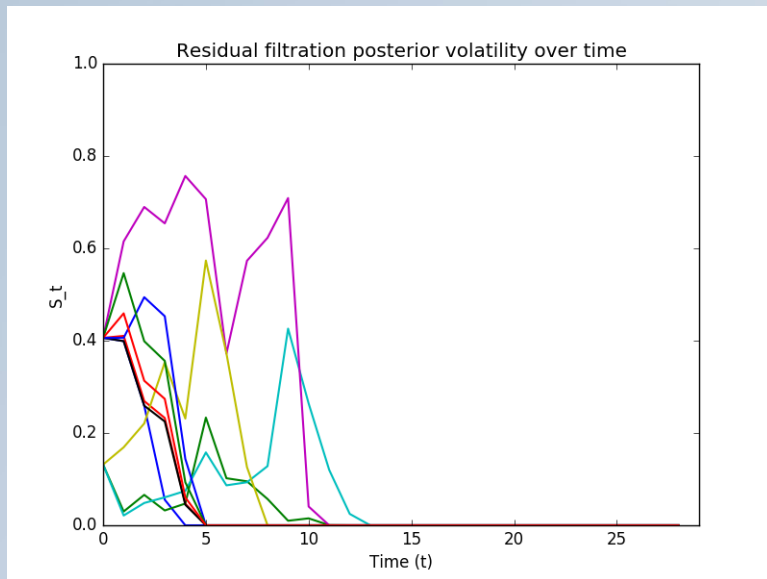
# Filtration results: all interactions



# Residual filtration posterior volatility

- A series of statistics to inform about the standard deviation over the filtration

$$s_t = \langle \text{std}\{P(W|\mathcal{F}(\tau))\}_{\tau=t:T} \rangle$$



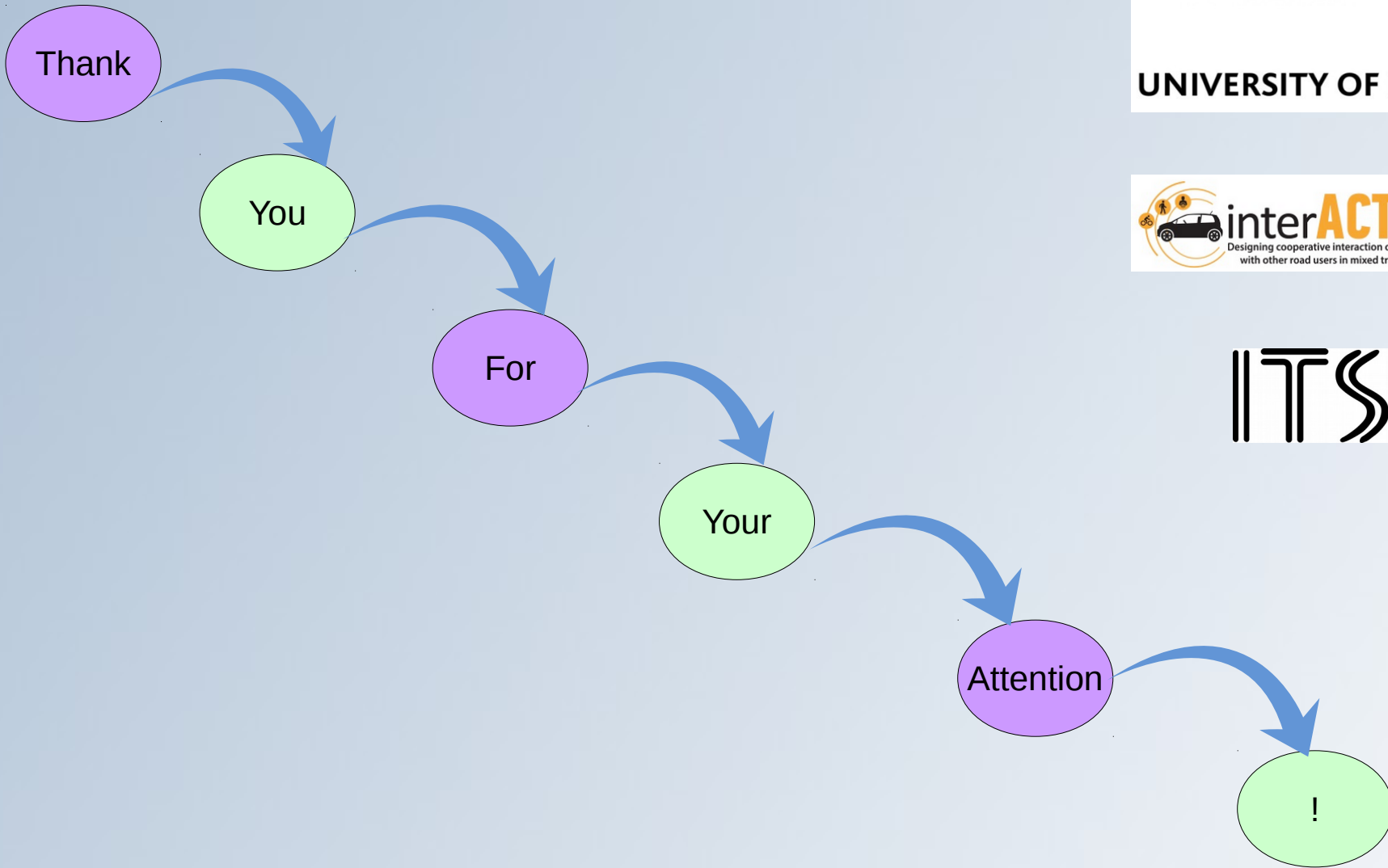
- The descriptor features and the first event features are important but not the later ones

# Conclusion

- Large scale observation of real world pedestrian-vehicle interactions
- Filtration on the sequences of interaction
- The residual shows that an Av should wait and observe the initial features before acting

# Future work

- Features are assumed to be independent => new way to model that
- Infer pedestrian and driver assertiveness:  $U_{\text{crash}}$  and  $U_{\text{time}}$
- Take into account observation of non-features



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